

In this post, I am going to explain the next combination technique around '過大実乘法' (Multiplication with Excessive multiplicand) called '過大実省一乘法.'

It is useful when the excessive-multiplicand is simpler than the multiplicand itself (as I explained in previous post) AND the initial digit of the multiplier is 1.

The principle:

When calculating $A*B$, if we add some value 'D' to multiplicand 'A' (the sum is called excessive-multiplicand 'E'), and eliminate the initial digit 1 from multiplier 'B' (let's call it 'M' for modified-multiplier), the expression would be:

$$\begin{aligned} A*B &= (E-D) * (10^n + M) \\ &= 10^n*(E-D) + E*M - D*M \end{aligned}$$

Since $10^n*(E-D)$ is on the board (although we have to mentally change the decimal point), all we have to do is add $E*M$ to the board, and subtract $D*M$ from it.

Example: $39698*157=6232586$

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ABC abcdefg
157 39698 : First, eliminate the initial 1 from the multiplier [A].
057 39698 : We are going to process '- D*M' term first,
           : so look at the other side of [e], which is 2,
           : multiply this value by [B] (5),
           : and subtract the result (10) from [ef].
057 39697 : then multiply 2 by [C] (7), and subtract the result (14) from [fg].
057 3969686 : Look at the other side of [c], which is 3,
           : multiply this value by [B] (5),
           : and subtract the result (15) from [cd].
057 3954686 : then multiply 3 by [C] (7), and subtract the result (21) from [ef].
057 3952586 : And now the process for '+ E*M',
           : so look at the top digit [a] (2) and realize
           : the excessive multiplicand is 40000,
           : multiply 4 by [B] (5) and add the result to [ab].
057 5952586 : then multiply 4 by [C] (7) and add the result to [bc].
057 6232586 : done.
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